

Statistics

Lecture 35



Feb 19-8:47 AM

Suppose ages of teachers in LAUSD are normally distributed with mean of 42 yrs and Standard dev. of 8 yrs. $N(42, 8)$

If we randomly select one teacher find the prob. that he/she is

a) below 50 yrs old.

$$P(X < 50)$$

$$= \text{normalcdf}(-E99, 50, 42, 8) = \boxed{.841}$$

b) more than 30 yrs old.

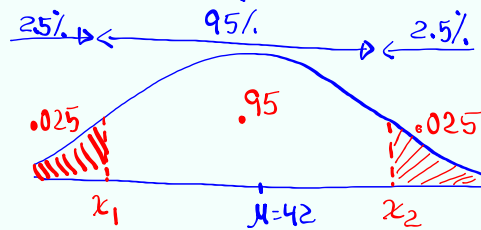
$$P(X > 30)$$

$$= \text{normalcdf}(30, E99, 42, 8)$$

$$= \boxed{.933}$$

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Find two ages, round to whole numbers that separate the middle 95% from the rest.



$$x_1 = \text{invNorm}(.025, 42, 8) \approx \boxed{26} \quad \mu = 42 \quad \sigma = 8$$

$$x_2 = \text{invNorm}(.975, 42, 8) \approx \boxed{58}$$

Recall usual Range

$$\mu \pm 2\sigma$$

95% Range

$$= 42 \pm 2(8)$$

$$= 42 \pm 16$$

$$\Rightarrow \boxed{26 \text{ to } 58}$$

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Consider the list below

1 3 5 7

Store in L1,

Find

use 1-Var stats

$$\mu = 4$$

with L1 only

$$\sigma = 2.236$$

$$\sigma^2 = 5$$

Take all samples with

Size 2 with replacement

Find \bar{x} of each sample

1,1	1,3	1,5	1,7	1	2	3	4
3,1	3,3	3,5	3,7	2	3	4	5
5,1	5,3	5,5	5,7	3	4	5	6
7,1	7,3	7,5	7,7	4	5	6	7

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1	2	3	4
2	3	4	5
3	4	5	6
4	5	6	7

16 means

\bar{x}	$P(\bar{x})$
1	1/16
2	2/16
3	3/16
4	4/16
5	3/16
6	2/16
7	1/16

$\bar{x} \rightarrow L2$
 $P(\bar{x}) \rightarrow L3$
 use 1-Var stats
 with $L2 \hat{=} L3$

$\mu = 4$
 $\sigma = 1.581$
 $\sigma^2 = 2.5 = \frac{5}{2}$

$$\mu_{\bar{x}} = \mu$$

$$\sigma_{\bar{x}}^2 = \frac{\sigma^2}{n}$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

Central-Limit
Theorem

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Clear all lists

Store the following
in L1

1 3 5 7 9

use 1-Var stats
with L1 only.

Take all Samples of
Size 2 with replacement

Find $\mu = 5$
 $\sigma = 2.828$
 $\sigma^2 = 8$

Find \bar{x} of each Sample

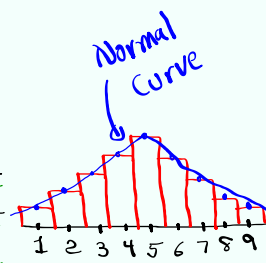
1,1	1,3	1,5	1,7	1,9	1	2	3	4	5
3,1	3,3	3,5	3,7	3,9	2	3	4	5	6
5,1	5,3	5,5	5,7	5,9	3	4	5	6	7
7,1	7,3	7,5	7,7	7,9	4	5	6	7	8
9,1	9,3	9,5	9,7	9,9	5	6	7	8	9

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1	2	3	4	5
2	3	4	5	6
3	4	5	6	7
4	5	6	7	8
5	6	7	8	9

25 means

\bar{x}	$P(\bar{x})$
1	$\frac{1}{25}$
2	$\frac{2}{25}$
3	$\frac{3}{25}$
4	$\frac{4}{25}$
5	$\frac{5}{25}$
6	$\frac{4}{25}$
7	$\frac{3}{25}$
8	$\frac{2}{25}$
9	$\frac{1}{25}$



$\bar{x} \rightarrow L2, P(\bar{x}) \rightarrow L3$
 Use $\boxed{1 - \text{VarStats}}$
 with $L2 \hat{=} L3$

CLT Says

$$\mu_{\bar{x}} = \mu$$

$$\sigma_{\bar{x}}^2 = \frac{\sigma^2}{n}$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

$\mu = 5$
 $\sigma = 2$
 $\sigma^2 = 4 = \frac{8}{2}$

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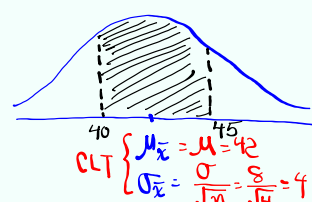
Ages of teachers in LAUSD are N.D.
 with $\mu = 42 \hat{=} \sigma = 8$.

If we randomly select 4 teachers,
 find $\mu_{\bar{x}} = \mu = 42$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{8}{\sqrt{4}} = \frac{8}{2} = 4$$

Find the Prob. that their mean age is
between 40 $\hat{=} 45$.

$P(40 < \bar{x} < 45)$
 $= \text{normalcdf}(40, 45, 42, 4)$
 $= \boxed{.465}$



CLT $\left\{ \begin{array}{l} \mu_{\bar{x}} = \mu = 42 \\ \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{8}{\sqrt{4}} = 4 \end{array} \right.$

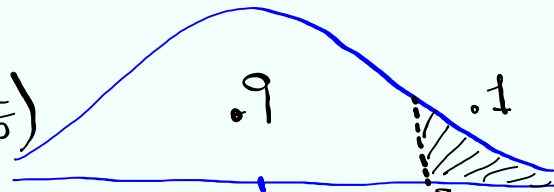
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Find the \bar{x} **mean age** for randomly selected groups of $n=5$ **5 teachers** that separate the **top 10%** from the rest.

Right area .1

$$\bar{x} = \text{invNorm}(.9, 42, 8/\sqrt{5})$$

$$\approx 46.585 \approx \boxed{47}$$



$$\text{CLT} \begin{cases} \mu_{\bar{x}} = \mu = 42 \\ \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{8}{\sqrt{5}} \end{cases}$$

Oct 31-9:42 AM

Salaries of nurses in LA county has a normal dist. with $\mu = \$7200$ and $\sigma = 500$.

If we randomly select 16 nurses,

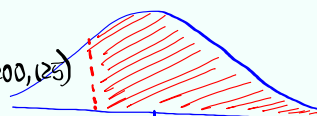
$$\text{CLT} \begin{cases} \mu_{\bar{x}} = \mu = 7200 \\ \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{500}{\sqrt{16}} = \frac{500}{4} = 125 \end{cases}$$

Find the Prob. that **their mean** salary is **more than \$7000**.

$$P(\bar{x} > 7000)$$

$$= \text{normalcdf}(7000, E99, 7200, 125)$$

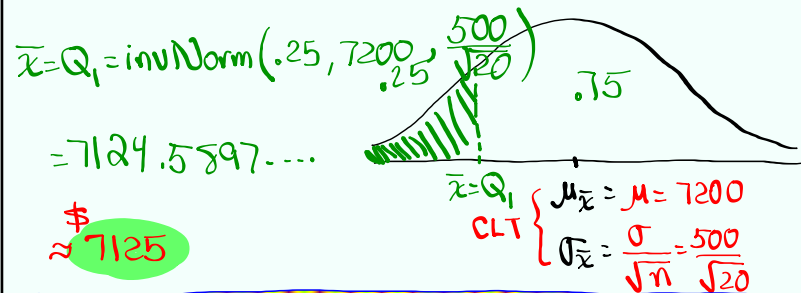
$$\approx \boxed{.945}$$



$$\text{CLT} \begin{cases} \mu_{\bar{x}} = \mu = 7200 \\ \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{500}{\sqrt{16}} = 125 \end{cases}$$

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find $\bar{x} = Q_1$ for randomly selected groups of
20 nurses. Round to whole #.



SG 18, 19, 20, and 21

Oct 31-9:53 AM